Tropical and Stratospheric Influences on Extratropical Short-Term Climate Variability

MATTHEW NEWMAN AND PRASHANT D. SARDESHMUKH

CIRES Climate Diagnostics Center, University of Colorado, and Physical Sciences Division, NOAA/Earth System Research Laboratory, Boulder, Colorado

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ABSTRACT

The relative impacts of tropical diabatic heating and stratospheric circulation anomalies on wintertime extratropical tropospheric variability are investigated in a linear inverse model (LIM) derived from the observed zero lag and 5-day lag covariances of 7-day running mean departures from the annual cycle. The model predicts the covariances at all other lags. The predicted and observed lag covariances are generally found to be in excellent agreement, even at the much longer lag of 21 days. This validates the LIM’s basic premise that the dynamics of weekly averages are effectively linear and stochastically driven, which justifies further linear diagnosis of the system.

Analysis of interactions among the LIM’s variables shows that tropical diabatic heating greatly enhances persistent variability over most of the Northern Hemisphere, especially over the Pacific Ocean and North America. Stratospheric effects are largely confined to the polar region, where they ensure that the dominant pattern of sea level pressure variability is the annular Arctic Oscillation rather than the more localized North Atlantic Oscillation. Over the North Atlantic, both effects are important, although some of the stratospheric influence is ultimately traceable to tropical forcing. In general, the tropically forced anomalies extend through the depth of the troposphere and into the stratosphere, whereas stratospherically generated anomalies tend to be largest at the surface and relatively weak at midtropospheric levels. Some persistent variability is, however, found even in the absence of these “external” forcings, especially near the amplitude maxima of the leading eigenmodes of the internal extratropical tropospheric evolution operator. One of these eigenmodes has a circumglobal zonal wavenumber-5 structure with maxima over the Arabian Sea and the central Pacific, and two others are associated with north–south dipole variations across the North Atlantic jet. Overall, tropical influences are generally found to be larger than stratospheric influences on extratropical tropospheric variability and have a pronounced impact on the persistent, and therefore the potentially predictable, portion of that variability.

1. Introduction

Extratropical atmospheric variability on time scales longer than a week, often called “low frequency” or short-term climate variability, is qualitatively different from daily synoptic variability. For example, during winter, synoptic variability is strongest in narrow regions north of the Atlantic and Pacific jets, whereas climate variability is largest in a broad region over the northeast Pacific. Also, synoptic weather systems are typically zonally oriented, whereas climate anomalies occur as north–south dipoles or follow great circle paths. These differences appear on time scales as short as a week. Natural climate variability on longer time scales is not fundamentally different from weekly variability, although it can differ in details (e.g., Kushnir and Wallace 1989; Feldstein 2000).

It is often suggested that climate variability reflects barotropic energy dispersion in a spherical atmosphere (Hoskins and Karoly 1981; Simmons 1982) in which anomalies are strongly influenced by the time-mean ambient flow (e.g., Simmons et al. 1983). Although this hypothesis was originally proposed in terms of the modal instability of the ambient flow, subsequent studies stressed energy extraction in preferred regions followed by propagation along preferred ray paths (e.g., Hoskins and Ambrizzi 1993; Borges and Sardeshmukh 1995; Branstator and Frederikson 2003). In such a scenario, some source of initial perturbations is needed, although substantial transient anomaly growth is still
possible. The simplest model incorporating this may be expressed as

$$\frac{dx}{dt} = Lx + F,$$

where \(x\) is a state vector representing extratropical tropospheric climate anomalies; \(L\) is a linear dynamical operator, which includes base-state interactions; and \(F\) represents forcing. For (1) to be a closed system, \(F\) can represent only stochastic forcing with externally specified amplitudes; otherwise, a second model of \(F\) would be needed.

Such a simple model can reproduce the gross features of observed low-frequency variance statistics if \(L\) is a linearized barotropic operator (e.g., Egger and Schill- ing 1983; Newman et al. 1997; Branstator and Frederik- son 2003). However, as Newman et al. (1997) stressed, it does a poor job of explaining the evolution of climate anomalies and related statistics, such as lag covariances. In particular, a linear barotropic model of the form (1) is a poor forecast model of short-term climate anomalies, worse than even persistence (Sardeshmukh et al. 1997; Winkler et al. 2001, hereafter WNS01). The reason for this is simple: the free barotropic eigenmodes have a relatively narrow range of decay rates but a wide range of phase speeds (e.g., Fig. 2 of Newman et al. 1997). A random forcing causes all the modes to be excited roughly equally on average, but their subsequent rapid dispersion leads to unrealistically small lag covariances. For (1) to produce realistic lag covariances in a barotropic framework, there has to be a process (e.g., a part of \(F\)) that is not random but rather acts to select some slowly evolving modes preferentially over others.

There are several ways to improve on the barotropic model while retaining the basic form of (1), although modified barotropic (Cai and Van den Dool 1991; Mit- tas and Robinson 2005) and simple baroclinic (WNS01) models have not proved much more successful in this regard. One possibility is to include linear synoptic eddy feedbacks (e.g., Lau 1988; Branstator 1995; Whi- taker and Sardeshmukh 1998) in \(L\), which, given that they are generally positive (Valdes and Hoskins 1989), would have a destabilizing effect on the lower-frequency eigenmodes of \(L\), making their selection easier. A second possibility is for \(F\) to include nonrandom “external” forcings of the extratropical tropospheric circulation, such as from the tropics and stratosphere. If these “forcings” are not entirely independent of \(x\) and/or each other, however, then one would need a linear model of the form (1), including linear interactions with other system components, for these forcings as well. In effect, one would then have a combined model of the form (1) for an augmented state vector \(x\) that includes these forcings as additional components but with \(F\) now again strictly random.

There is, of course, also the possibility that the form (1) itself is incorrect, especially given the suggestion of nonlinear low-frequency behavior (e.g., Kimoto and Ghil 1993; Corti et al. 1999). The dynamics of some nonlinear systems with “slow” and “fast” components can, however, be approximated by linear deterministic dynamics plus stochastic white noise forcing if the nonlinearities decorrelate sufficiently rapidly relative to the time scales of forecast interest (e.g., Papanicolaou and Kohler 1974; Hasselmann 1976; Penland 1996). In such systems, the predictable parts of future states are associated with purely linear and/or linearly parameterizable dynamics, so the system is effectively linear (New- man et al. 2003) and can be approximated by (1) with \(F = \xi\) as a white noise forcing (which may or may not have geographical structure). In Part I of this work (WNS01), we derived such an effectively linear dynamical model from observations. The model was shown to have good forecast skill (WNS01; Newman et al. 2003), and predictability estimates derived from it were shown to be consistent both with its own actual forecast skill and, more important, with that of a (bias corrected) version of the medium-range forecast model used operationally at the National Centers for Environmental Prediction in 1998 (Newman et al. 2003).

Many previous studies have considered either tropical or stratospheric influences on extratropical tropospheric variability, but generally not both. For example, the state vector considered by WNS01 (including weekly extratropical tropospheric streamfunction and tropical diabatic heating anomalies) did not allow an evaluation of the relative importance of the tropical and stratospheric influences. This is increasingly be- coming an important issue given, for example, the evidence of both tropical (Sardeshmukh et al. 2000; Hoorling et al. 2001; Lin et al. 2002; Branstator 2002; Zhou and Miller 2005; Bader and Latif 2005) and strato- spheric (Baldwin and Dunkerton 2001; Ambaum and Hoskins 2002; Thompson et al. 2002) influences on the North Atlantic Oscillation (NAO). There is also some recent evidence that observed stratospheric variability is related to ENSO (e.g., Camp and Tung 2007; Wei et al. 2007) and that such variability can be reproduced by GCMs with prescribed observed sea surface tempera- tures (e.g., Lahoz 2000; Taguchi and Hartmann 2006; Manzini et al. 2006). This raises the possibility that at least some extratropical tropospheric effects previously attributed to stratospheric influences may ultimately be traceable to tropical forcing. On the other hand, some
stratospheric influences may also have been implicitly included in WNS01’s empirically derived L operator, possibly leading to an overstatement of tropical influences in their study.

Thus, our principal aim in this paper is to compare the impacts of tropical heating and stratospheric circulation anomalies on short-term extratropical tropospheric climate variability, including that at the surface, in a single dynamical framework. To this end we will extend the linear inverse model (LIM) of WNS01 by including stratospheric streamfunction and sea level pressure as part of the model state vector, as described in section 2. We consider an explicit treatment of stratospheric streamfunction, as the surface at the tropics. The EOFs of tropospheric streamfunction anomalies are more pronounced at the surface than at midtropospheric levels (e.g., Baldwin et al. 2003; Thompson et al. 2006). In section 3, we show that our extended LIM’s forecast skill is as good as or better than that of WNS01’s LIM. As a further key demonstration of linearity justifying our linear diagnosis here, we show that the LIM reproduces the observed lag covariances at much longer lags than the lag at which it is trained. In section 4, both tropical diabatic heating and stratospheric influences are shown to be crucial for this successful reproduction, although the tropical effect is dominant over the Pacific sector and throughout the midtroposphere, whereas stratospheric effects are largest at the surface of the Arctic and, apart from the North Atlantic, are less significant elsewhere. More detailed diagnosis of the differing tropical and stratospheric impacts on tropospheric anomaly amplification and forecast skill is presented in section 5. Diagnosis of tropical impacts upon stratospheric variability is presented in section 6. Some issues relating to the LIM’s relatively poor performance at the surface over some of the North Atlantic are discussed in section 7, and concluding remarks are made in section 8.

2. Model details and data

The model state vector \( \mathbf{x} \) in (1) is

\[
\mathbf{x} = \begin{bmatrix}
\mathbf{p} \\
\psi_T \\
\mathbf{H} \\
\psi_S
\end{bmatrix},
\]

where \( \mathbf{p} \) is sea level pressure (SLP), \( \psi_T \) is tropospheric streamfunction, \( \mathbf{H} \) is tropical diabatic heating, and \( \psi_S \) is stratospheric streamfunction. All quantities represent 7-day running mean anomalies. Thirty-five years (from 1968/69 to 2002/03) of wintertime (1 December–28 February) NCEP-National Center for Atmospheric Research (NCAR) reanalysis data were used to define \( \mathbf{x} \). The diabatic heating rates were determined from an improved iterative solution of the “\( \chi \) (chi) problem” (Sardeshmukh 1993; Sardeshmukh et al. 1999), as described in WNS01. All variables were spectrally truncated to T21 and transformed onto a Gaussian grid; this truncation affects none of our results. Low-frequency anomalies were defined by removing each variable’s annual cycle, defined by running a 31-point smoother on the daily climatology of the low-pass data, at each grid point from the weekly means. Constructing anomalies in this manner gave virtually identical results to the slightly different method used by WNS01. Tropospheric streamfunction anomalies \( \psi_T \) were determined at 250 hPa (\( \psi_{T250} \)) and 750 hPa (\( \psi_{T750} \)), and stratospheric streamfunction anomalies \( \psi_S \) at 30 hPa; similar results (not shown) were obtained by defining \( \psi_T \) at 70 hPa. Diabatic heating anomalies were smoothed using a T21 spectral filter that attenuates small-scale features and the Gibbs phenomena (Sardeshmukh and Hoskins 1984).

The anomaly fields were projected onto their leading empirical orthogonal functions (EOFs). As in WNS01, all EOFs were determined for the Northern Hemisphere (NH) except for diabatic heating EOFs, which were determined for the region 30°S–30°N. Prior to computing EOFs, each anomaly field was normalized by its domain-averaged climatological root-mean-square amplitude. The EOFs of tropospheric streamfunction were computed from a vector combining the normalized \( \psi_{T250} \) and \( \psi_{T750} \) anomalies rather than at each level separately. Figure 1 shows the leading two EOFs of \( \psi_T \) (displayed only at 250 hPa), \( \mathbf{p} \), \( \psi_S \), and \( \mathbf{H} \), and the fractional variances of these fields explained by them. The EOFs of \( \psi_T \) and \( \mathbf{H} \) are essentially the same as in WNS01. The leading \( \mathbf{p} \) EOF, or \( \mathbf{p} \)/EOF1, shows the well-known Atlantic pattern variously termed the North Atlantic Oscillation (NAO) (e.g., Deser 2000; Ambaum et al. 2001) or the Arctic Oscillation (AO) (e.g., Thompson and Wallace 2000). It is also often referred to as an “annular mode” but, at least for 7-day means, this EOF has a strong wavenumber-1 component. The \( \psi_S \)/EOF1 is strongly associated with the quasi-biennial oscillation (QBO), including relatively strong zonally symmetric zonal wind anomalies in the tropics and around 70°N (Holton and Tan 1982; Randel et al. 1999), and a corresponding principal component dominated by (though not exclusively comprising) variations of roughly 2-yr period. Note that the patterns in Fig. 1 do not represent EOFs of the combined fields,
FIG. 1. Leading EOFs of selected variables used in the model for (left) EOF 1 and (right) EOF 2: (top) 30-hPa streamfunction ($\psi_{30}$), (second row) 250-hPa streamfunction ($\psi_{250}$), (third row) SLP (p), and (bottom) tropical heating (H). Contour intervals are arbitrary but the same for EOFs 1 and 2. The overall sign is also arbitrary: one sign is gray shading and thick contours, and the other sign is thin contours. Zero contours in this and all subsequent figures (except Fig. 2) are removed for clarity.
so, for example, \( \psi_f / \text{EOF1} \) corresponds best to \( p / \text{EOF2} \) and \( p / \text{EOF1} \) corresponds best to \( \psi_f / \text{EOF4} \) (not shown).

The leading 40, 24, 18, and 4 EOFs of \( \psi_f, p, H, \) and \( \psi_c \) were retained, explaining about 90%, 90%, 55%, and 84% of the variability of these fields. The time-varying coefficients of these EOFs, that is, the principal components (PCs), define our 86-component state vector \( x \). Note that we retain substantially more tropical diabatic heating variance than WNS01 because we did not encounter the Nyquist lag problem that they encountered, possibly because of our use of 4× daily data, as opposed to their 2× daily data. As in WNS01, a training lag of \( \tau_o = 5 \) days was used to estimate \( L \) from the relationship \( C(\tau_o) = \exp(L\tau_o)C(0) \), where \( C(\tau) = (x(t + \tau)x^T(t)) \). The EOF truncations and training lag were chosen to maximize the LIM cross-validated forecast skill (see below and WNS01). In no other respect do our choices of training lag and EOF truncations affect the points made in this paper. Minor sensitivities of the results to these choices were similar to those reported in WNS01, so are not repeated here.

3. Evaluating the LIM

Figures 2b and 2d show the LIM’s forecast skill, measured in terms of local anomaly correlation between the untruncated observations and the week 3 forecasts of \( \psi_{250} \) and \( p \) that were cross-validated (i.e., verified on independent data) as described in WNS01. The full LIM’s skill in Fig. 2 is similar to that of WNS01’s LIM. Extending the LIM’s state vector with \( p \) and \( \psi_c \) components improves neither \( \psi_f \) nor \( H \) skill (not shown, but see Newman et al. 2003), as is clear from comparison with a LIM derived from \( \psi_f \) and \( H \) alone (“\( \psi_f / H \) LIM”; cf. Figs. 2a and 2b) as in WNS01. On the other hand, a “\( p/\psi_f \) LIM” derived from \( p \) and \( \psi_f \) alone is generally much less skillful than the full LIM at forecasting \( p \) (cf. Figs. 2c and 2d). The exception is over the polar and North Atlantic regions. Most of the polar \( p \) skill is due to \( \psi_c \); for LIMs constructed without \( \psi_c \) (not shown), polar \( p \) skill is only \( \sim 0.15 \) (except 0.3 around 30°E). This result is consistent with earlier studies of statistical surface forecast skill dependence upon the stratosphere where the predictand was either the AO (Baldwin et al. 2003; Charlton et al. 2003) or zonal mean zonal wind at 60°N (Christiansen 2005). On the other hand, most of the North Atlantic \( p \) skill can also be obtained from a LIM constructed from \( p \) alone (not shown).

WNS01 showed that their LIM could reproduce a broad measure of lagged covariance, the trace of the lag autocovariance matrix (proportional to the lag-autocovariance averaged over all PCs), for lags up to 30 days. Next, we perform a more detailed comparison of the predicted and observed lag-autocovariances in grid space. This is a key test of linearity since (1) implies that \( C(\tau) = G(\tau)C(0) \), with \( G(\tau) = \exp(L\tau) \).

Figure 3 compares the observed 21-day lag-autocovariances of \( \psi_{250} \) and \( p \) with the LIM predicted values. The results for \( \psi_{250} \) are intermediate between those for the surface and 250 hPa and, therefore, are not shown. The LIM prediction is best at 250 hPa (Fig. 3, top), especially over the Pacific. The relatively minor differences over the Atlantic are well within sampling uncertainty (see section 7). These errors are very small compared to the corresponding errors of a two-level linear balance model described in WNS01, which produces weak negative 21-day lag-autocovariances throughout the hemisphere (not shown). The LIM predicted lag-autocovariances of \( p \) (Fig. 3, middle) are also realistic over the Pacific, although the observed region of high persistence extends about 10° farther west. The LIM captures the locations and amplitudes of all other extrema, with the clear exception of the \( p \) maximum over the North Atlantic. This difference is apparently unrelated to discrepancies in the LIM’s stratospheric (not shown) and tropical heating lagged autocovariances (Fig. 3, bottom), which are rather small apart from an underestimation of tropical heating persistence in the central equatorial Pacific (see section 7). In fact, tropical heating is critical to the LIM’s success here: only LIMs whose state vector explicitly includes \( H \) can reproduce the observed magnitude of extratropical lag autocovariance for lags greater than two weeks.

Regions of relatively large lag-autocovariance also tend to be regions of persistent anomalies and, therefore, of relatively large low-frequency variance. One can make a more direct comparison of the LIM’s predicted low-frequency variance with observations, either by computing the power in desired frequency bands directly from (1), as in Penland and Ghil (1993), or by making a long run of (1) and collecting statistics. We followed the latter approach, integrating (1) forward for 50,000 days using the method described in Penland and Matrosova (1994). The white noise forcing \( \xi = \sum_j q_j \eta_j f_j(t) \) was specified using independent Gaussian white noises \( f_j(t) \) with unit variance, and \( q_j \) and \( (\eta_j)^2 \) as the eigenvectors and eigenvalues, respectively, of the positive-definite noise covariance matrix \( Q = (\xi E)^{-1} dt \), estimated using the fluctuation–dissipation relationship,

\[
dC(0)/dt = 0 = LC(0) + C(0)L^T + Q,
\]

to solve for \( Q \) given the observed \( C(0) \) and \( L \). This solution is guaranteed to be symmetric but not positive.
definite. Indeed, we found four small negative eigenvalues of $Q$ accounting for less than 1% of the trace of $Q$. Following Penland and Matrosova (1994), we produced a legitimate modified noise covariance matrix by setting those negative eigenvalues to zero, rescaling the remaining positive eigenvalues to preserve the total forcing variance, and reconstructing $Q$ using the rescaled eigenvalues and corresponding eigenvectors. This reconstruction resulted in an increase of noise variance just southeast of Greenland. Finally, a modified $C(0)$ consistent with (1) was recalculated from (2) by specifying $L$ and the modified $Q$. The impact of this modification was small, as can be seen by comparing the observed (Fig. 4, top left) and modified (Fig. 4, middle left) $\psi_{250}$ variance maps. Note that these would be identical (apart from the EOF truncation) if $Q$ had not been modified.

We constructed 21-day running means from the long LIM run by averaging sets of three values, each spaced 7 days apart. The resulting comparison of LIM-predicted variance of 21-day means to the observed variance of 21-day means (Fig. 4, right) is encouraging because it is a harder test for the LIM than the comparison of total variance, since it tests the spectral distribution of the variance, that is, the fidelity of the simulated power spectrum.
4. Tropical and stratospheric influences on persistent variability

Following the approach of Newman et al. (2000), the relative importance of tropical heating and stratospheric influences in extratropical tropospheric dynamics may be investigated in a framework in which (1) is rewritten as

\[
\frac{d}{dt} \begin{bmatrix} x_T \\ H \\ \psi_S \end{bmatrix} = \begin{bmatrix} L_{TT} & L_{TH} & L_{TS} \\ L_{HT} & L_{HH} & L_{HS} \\ L_{ST} & L_{SH} & L_{SS} \end{bmatrix} \begin{bmatrix} x_T \\ H \\ \psi_S \end{bmatrix} + \begin{bmatrix} \xi_T \\ \xi_H \\ \xi_S \end{bmatrix},
\]

where \( x_T \) represents the tropospheric circulation subvector, which now includes \( \psi_T \) and \( p \). Note that \( L_{TT} \) is distinct from a linear operator (say, \( L_{TT}' \)) obtained from a LIM of \( x_T \) alone. The latter would implicitly include linear diagnostic relationships between \( x_T \), and \( H \) and \( \psi_S \). By explicitly separating out the effects of \( H \) and \( \psi_S \) on \( x_T \), (3) enables us to identify \( L_{TT} \) more cleanly with “internal” extratropical tropospheric dynamics. Of course, \( L_{TT} \) may still implicitly retain the influence of variables not included in \( x \).

To make an overall assessment of the “external” tropical heating and stratospheric influences on extra-
FIG. 4. Variance of 250-hPa streamfunction ($\psi_{250}$) for (left) 7-day running means and (right) 21-day running means: (top) Observed, (middle) from LIM, and (bottom) from LIM with the “forcing” terms (heating and stratosphere) removed. Contour interval is $4.5 \times 10^{13}$ m$^4$ s$^{-2}$ ($3 \times 10^{13}$ m$^4$ s$^{-2}$) in the left (right) panels.
tropical tropospheric variability, we made another 50,000-day run of the system:

$$\frac{d\mathbf{x}_T}{dt} = \mathbf{L}_{TT} \mathbf{x}_T + \xi_T.$$  (4)

The bottom left of Fig. 4 shows the variance of $\psi_{250}$ obtained in this run. As expected, removing the external influences decreases the variance, although this change is generally far smaller over the Atlantic than the Pacific. Similar results are obtained for $\mathbf{p}$ (not shown). Removing the external influences has a larger impact on the variance of the 21-day means, as shown in the bottom right panel of Fig. 4. However, the impacts over the central Pacific and North Atlantic remain small even at these longer time scales.

Further isolation of the tropical heating and stratospheric influences is possible by considering two modified $\mathbf{L}$ operators: $\mathbf{L}_\text{noh}$ in which $\mathbf{L}_{TH} = \mathbf{L}_{HT} = \mathbf{L}_{SH} = \mathbf{L}_{HS} = 0$ and $\mathbf{L}_\text{nos}$ in which $\mathbf{L}_{TS} = \mathbf{L}_{ST} = \mathbf{L}_{HS} = \mathbf{L}_{SH} = 0$. The predicted lag covariances using these modified operators are $\mathbf{C}_\text{noh}(\tau) = \exp(\mathbf{L}_\text{noh} \tau) \mathbf{C}(0)$ and $\mathbf{C}_\text{nos}(\tau) = \exp(\mathbf{L}_\text{nos} \tau) \mathbf{C}(0)$. Results for the 21-day lag-autocovariances are shown in Fig. 5. For reference, the top panels of Fig. 5 repeat the full LIM predictions for $\psi_{250}$ (left) and $\mathbf{p}$ (right) from Fig. 3. The much weaker lag covariance obtained without tropical heating (Fig. 5, middle) shows that the heating is responsible for most of the observed persistent variability over most of the domain, whereas the stratospheric impact (Fig. 5, bottom) is generally minor. At the surface over the North Atlantic and polar regions, however, the picture is more mixed, with tropical heating responsible for much of the persistence over the far North Atlantic but the stratosphere responsible for about half of the persistence in the Arctic north of Siberia, near the positive center of $\mathbf{p}$/EOF1 (cf. Fig. 1). At longer lags, such as 35 days (not shown), over the far North Atlantic, the stratospheric impact increases to equal that of tropical heating.

Although removing these external influences generally diminishes the persistence of extratropical tropospheric anomalies, some persistence remains, especially over the Atlantic and near the date line in the Pacific (see bottom right panel of Fig. 4 and middle left panel of Fig. 5). This persistence cannot be captured by a stochastically forced two-level linear balance model of extratropical dynamics (not shown). It is, however, linked to the least damped eigenmodes of our empirically determined “internal” extratropical dynamical operator $\mathbf{L}_{TT}$. For example, the pattern of persistence over the Atlantic is consistent with the structures of the two leading eigenmodes of $\mathbf{L}_{TT}$, shown in Figs. 6a and 6b for $\psi_{250}$ (other levels not shown). Both modes are stationary north–south dipoles straddling the Atlantic jet with $e$-folding decay times of about three weeks (much shorter than for the leading eigenmodes of the full $\mathbf{L}$ operator). The first tilts westward with height and the second, which strongly resembles the NAO at the surface, is barotropic. These Atlantic eigenmodes are quite different from the leading eigenmodes of simple barotropic or baroclinic models linearized about the time-mean basic state. This suggests that synoptic-eddy feedbacks, which are in effect parameterized in $\mathbf{L}_{TT}$, modify those eigenmodes so as to enhance persistence, primarily over the Atlantic.

The most energetic phase of the third eigenmode of $\mathbf{L}_{TT}$, with maximum amplitude in the Pacific sector, is a circumglobal pattern (Fig. 6c) similar to that in Branstator (2002) except for relatively weak amplitude in the North Atlantic. It is remarkable how well the amplitude maxima of this circumglobal mode match the maxima of the simulated persistent variability without external tropical and stratospheric influences (cf. Fig. 6c to the bottom right panel of Fig. 4 and middle left panel of Fig. 5). The least energetic phase of this eigenmode (not shown), a weak zonally elongated north–south dipole straddling the west Pacific jet, is effectively distinct from the circumglobal pattern since the eigenmode has a 200-day period, longer than three $e$-folding times. Unlike in Fig. 6b, there is no dipole mode straddling the Pacific jet exit.

It is interesting that no single eigenmode of the full $\mathbf{L}$ operator can be identified with the unforced circumglobal mode, although a few eigenmodes (not shown) do have maxima in some of the same locations. Perhaps the closest is the fourth eigenmode, whose tropical heating component resembles the $\mathbf{H}$/EOF2 and whose extratropical structure combines aspects of the unforced circumglobal mode (Fig. 6c) with the second unforced Atlantic mode (Fig. 6b). This fourth mode is also very similar to a pattern obtained by regressing winter-mean upper-level streamfunction anomalies on the leading principal component of low-level North Atlantic streamfunction anomalies (Branstator 2002).

The tropospheric covariance budget, which may be expressed using (2) and (3) in the form

$$[\mathbf{L}_{TT} \mathbf{C}_{TT} + \mathbf{C}_{TT} \mathbf{L}_{TT}^\top] + [\mathbf{L}_{TH} \mathbf{C}_{HT} + \mathbf{C}_{HT} \mathbf{L}_{TH}^\top] + [\mathbf{L}_{TS} \mathbf{C}_{ST} + \mathbf{C}_{ST} \mathbf{L}_{TS}^\top] + \mathbf{Q}_{TT} = \mathbf{0}. \quad (5)$$
where $C_{xy} = \langle xy^T \rangle$ provides an alternative method of isolating the importance of tropical and stratospheric influences on extratropical tropospheric variability. Figure 7 shows the diagonal elements corresponding to $\psi_{250}$ of each of the bracketed terms in this budget, which may be interpreted as their contribution to the local $\psi_{250}$ variance tendency. It should be kept in mind that, although these terms relate to the maintenance of local variance, they contain nonlocal effects: $L_{TT}$ and $C_{TT}$ are not diagonal matrices, and tropical heating and stratospheric circulation variability contribute to tropospheric streamfunction variability. The primary balance in Fig. 7 is between the stochastic noise forcing, which acts to maintain the variance, and the internal tropo-

![Fig. 5. Comparison of the effects of tropical heating ($H$) and stratospheric streamfunction ($\psi_s$) upon 21-day lag covariance: (left) 250-hPa streamfunction ($\psi_{250}$) lag covariance and (right) SLP ($p$) lag covariance. Contour interval and shading as in Fig. 3.](image-url)
spheric dynamical terms, whose net effect is to dissipate it (hence “fluctuation–dissipation”). Over most of the hemisphere, the tropical heating generates less variance than the noise forcing, except in Rossby wave source regions in the subtropics (Sardeshmukh and Hoskins 1988). The stratospheric influence is again generally small. Similar results are obtained for the SLP variance (not shown), except that the stratospheric effect is slightly stronger and has centers over Scandinavia, Greenland, and Siberia.

It is interesting to break down the internal tropospheric term in Fig. 7 further into “local” and “nonlocal” contributions. The local contribution is associated with the product of the diagonal elements of $L_{TT}$ with the corresponding diagonal elements of $C_{TT}$, and the nonlocal contribution with the difference of the local contribution from the total internal tropospheric term. As expected, the local contribution is dissipative with an $e$-folding decay time scale ranging from $\sim 3.5$ days over land and the far western Pacific to $\sim 5$ days over the oceans, except for $\sim 6$ days over the far North Atlantic and Arctic Oceans (cf. Fig. 4). The nonlocal term, generally positive owing to the destabilization of low-frequency anomalies through interactions with the time-mean basic state (e.g., Simmons et al. 1983; Borges and Sardeshmukh 1995) as well as positive synoptic-eddy feedbacks (Valdes and Hoskins 1989; Whitaker and Sardeshmukh 1998), offsets the local dissipation, but falls well short of overcoming it.

5. Tropical and stratospheric influences on rapidly amplifying structures

To better understand the results of the previous section, it is useful to examine tropical and stratospheric influences on the evolution of large-amplitude and long-lasting tropospheric anomalies. To this end, we consider the singular vector decomposition (SVD) of the system propagator $G(\tau) = \exp(\mathbf{L}\tau)$ under various norms and lead times $\tau$, which yields a dominant pair $u_1, v_1$ of normalized singular vectors associated with the maximum singular value $\lambda_1$ (e.g., Farrell 1988; Sardeshmukh et al. 1997). This identifies the “optimal” initial condition $v_1$ leading to the largest anomaly $G_{v_1} = \lambda_1 u_1$ at time $\tau$ (under a chosen norm). Newman et al. (2003) suggested that weekly extratropical anomalies should be most predictable when there is a large initial projection on $v_1$. The maximum possible anomaly growth factors $\lambda_1^2$, determined separately for each model variable in the $L2$ norm (i.e., domain-mean-square amplitude), are displayed as functions of $\tau$ in Fig. 8 as “maximum amplification” (MA) curves (Penland and Sardeshmukh 1995). The results for $\psi_T$ are qualitatively similar.

![Fig. 6. The 250-hPa streamfunction ($\psi_{250}$) portion of the three leading eigenmodes of $L_{TT}$: (a) Least damped eigenmode, (b) second eigenmode, and (c) third eigenmode, the most energetic phase. Contour interval and overall sign are arbitrary. Countours/shading are as in Fig. 1.](image-url)
FIG. 7. The local variance budget for 250-hPa streamfunction (see text for description of terms). Note that the sum within the green shaded region is zero, and the panel in the upper left corner is equal to the sum in the white shaded regions. Contour and shading interval is $6 \times 10^{12} \text{ m}^4 \text{ s}^{-2} \text{ day}^{-1}$; positive values are shaded in yellow/red tones and negative in blue.
to those found earlier by WNS01 but since our system is higher dimensional than in WNS01, it has the potential for larger amplification. Note that the peak in the MA curve occurs earlier for $\mathbf{p}$ than for $\psi_T$, suggesting that the predictability of $\mathbf{p}$ might also peak earlier than that of $\psi_T$, consistent with the lower 21-day $\mathbf{p}$ forecast skill (Fig. 2).

These different curves also correspond to the different optimal initial and final states associated with the maximum possible growth of each model variable. For example, maximizing the amplification of $\psi_T$/EOF1 over a 21-day interval requires an optimal initial condition dominated by large tropical heating anomalies, as WNS01 found earlier for growth under the global $\psi_T$ norm. In fact, the response (Fig. 9a), to just the initial tropical anomaly in our case is only somewhat weaker than the response to the full optimal initial condition (not shown). On the other hand, maximizing the amplification of $\mathbf{p}$/EOF1 requires a very different initial condition, including larger initial stratospheric polar and tropospheric North Atlantic anomalies (not shown). In this case, the 21-day response (Fig. 9b) is mostly due to the extratropical portion of the optimal initial condition. Tropical heating plays a secondary role in the growth of $\mathbf{p}$/EOF1 for leads this short. Note that maximizing the amplitude of $\mathbf{p}$/EOF1 does not result in a correspondingly large midtropospheric anomaly. In general, we find that maximizing amplification of surface anomalies tends to coincide with relatively weaker midtropospheric amplification, and vice versa.

Obviously, the atmosphere does not care which norm we choose. However, when making a forecast, some variables may be of more interest than others, in which case initial conditions leading to large anomalies in those variables become of interest. The choice of norm is then no longer arbitrary, and an SVD analysis of $\mathbf{G}$ under that norm can provide valuable insight into potential forecast skill. For example, amplification (and potential predictability) of $\psi_T$ is potentially larger than of $\mathbf{p}$ (Fig. 8). Likewise, Fig. 10 shows that the cross-validated anomaly correlation skill of LIM forecasts, for leads up to 30 days, is generally higher for the leading PCs of $\psi_T$ than for the leading PCs of $\mathbf{p}$.

Also shown in Fig. 10 is the skill of forecasts in which the initial anomalies of either $\mathbf{H}$ or $\psi_S$ are set to zero. Note that this is not quite the same as making forecasts using the modified operators $\mathbf{L}_{\text{noh}}$ and $\mathbf{L}_{\text{nos}}$ discussed in section 4, since the full LIM used here can subsequently generate $\mathbf{H}$ and/or $\psi_S$ anomalies that subsequently affect other forecast variables. In other words, instead of assessing the effect of entirely removing tropical or
FIG. 9. (a) Day-21 response to the tropical portion (30° S–30° N) of the optimal initial condition for maximizing the amplitude of $\psi_{30}$/EOF1. (b) Day-21 response to the extratropical portion (35°–90° N) of the optimal initial condition for maximizing the amplitude of $p$/EOF1. The full optimal initial condition in both cases is normalized to unity. Contour intervals: (top) 30-hPa streamfunction ($\psi_{30}$, 3.75 $\times$ 10$^4$ m$^2$ s$^{-1}$), (middle) 250-hPa streamfunction ($\psi_{250}$, 2.5 $\times$ 10$^5$ m$^2$ s$^{-1}$), and (bottom) SLP ($p$, 20 Pa). Positive (negative) values are indicated by shading and thick contours (thin contours).
stratospheric influences, we determine how a large initial \( \mathbf{H} \) or \( \psi_S \) anomaly (or error) can impact a forecast using the full LIM. Figure 10 shows that \( \mathbf{p} \) (\( \psi_T \)) PC1 skill is reduced by ignoring initial stratospheric (tropical heating) anomalies but is almost unaffected by ignoring initial tropical heating (stratospheric) anomalies, again as we might expect from the SVD results in Fig. 9. Ignoring initial heating anomalies degrades the PC2 skill for both variables, whereas ignoring initial stratospheric anomalies has no effect.

6. Tropical influences on stratospheric variability

Up to this point, we have treated the tropical and stratospheric influences as independent influences on extratropical tropospheric variability. In fact, as is im-
plied by (3) and seen in Fig. 9a, tropical forcing also affects stratospheric variability. For example, approximately one-third of the variance of $\psi_5$ is due to the tropical portion of the linear operator. Also, ignoring initial $H$ anomalies in all forecasts reduces $\psi_5$ PC2 forecast skill by as much as 0.1 at longer than 25-day lead times. Interestingly, the initial $H$ anomaly associated with the maximum amplification of $\psi_5$/EOF2, shown in Fig. 11, is not particularly ENSO- or MJO-like. Such an initial $H$ anomaly can, by itself, produce a pronounced weakening of the stratospheric polar vortex, particularly over Hudson Bay, in 21 days (Fig. 11, top).

If stratospheric anomalies can be forced by tropical heating, then some tropospheric impacts attributed to the stratosphere may be ultimately due to tropical heating. To investigate this possibility, a separate LIM operator $L$ was constructed for $\psi_T$/$\psi_5$ (i.e., by dropping $H$ from $x$) and used to compute both $C(\tau) = \exp(L\tau)C(0)$ and $\tilde{C}_{\text{nos}}(\tau) = \exp(L_{\text{nos}}\tau)C(0)$. Removing stratospheric influences from this LIM (as in Fig. 5) had as large an impact on North Atlantic and polar $p$ lag covariability as did the combined removal of tropical and stratospheric influences from the full LIM. This suggests that the actual stratospheric impact on the troposphere is overestimated when the LIM analysis does not also explicitly consider tropical heating.

How some tropical effects might falsely be attributed to the stratosphere is illustrated by examining tropical and stratospheric anomalies associated with optimal $p$ anomaly growth over long time intervals. For example, the full optimal initial condition for amplification of $p$/EOF1 over 35 days (not shown) is similar to that, which in 21 days, evolves into Fig. 9b, but with greater $H$ and $\psi_5$ amplitudes and lesser $\psi_T$ and $p$ amplitudes. By day 35, it evolves into an AO-like SLP anomaly with a pronounced stratospheric anomaly (i.e., as $\exp(L_{\text{35}})\mathbf{v}_1$; Fig. 12, left panels). If, instead, the same initial condition is allowed to evolve without any interactions with the tropical heating [i.e., as $\exp(L_{\text{noh}}\text{35})\mathbf{v}_1$], the result (Fig. 12, right panels) is not only a much weaker $p$ anomaly but also a much weaker $\psi_5$ anomaly. The tropical heating is, thus, largely responsible for the amplification of both surface and stratospheric anomalies in this case. Still, without stratospheric feedbacks [i.e., using $\exp(L_{\text{noh}}\text{35})\mathbf{v}_1$, not shown], the amplified response is confined between 90°W and 90°E, suggesting that stratospheric feedbacks are responsible for the annual nature of the response in high latitudes. The importance of stratospheric feedback to $p$ anomalies over Siberia is also consistent with the pronounced surface temperature–stratospheric vortex relationship noted there by Thompson et al. (2002).

It is gratifying that the LIM reproduces the observed 21-day lag-autocovariances over most of the Northern Hemisphere, as shown in section 3, despite inevitable errors associated with using real-world observations. In view of this overall success, the LIM’s error in Fig. 3 over the area extending from the North Atlantic to the Barents Sea is notable. This discrepancy is more pronounced at the longer lags of 28 days and 35 days, as shown in Fig. 13. The LIM underestimates SLP persistence over the North Atlantic and overestimates it over the Barents Sea. Interestingly, this departure is limited to the surface. Errors in $\psi_{250}$ (Fig. 13, top panels) and $\psi_{750}$ (not shown) persistence are small and statistically insignificant, both locally and in a “field significance” sense, even at the 90% level (this was determined from 1000 Monte Carlo trials, in each of which the lag-autocovariance was computed from a dataset constructed by resampling the 35 winters with replacement). The surface error appears to have a coherent spatial structure, but it does not resemble any of the $p$ EOFs, and the variations of $p$ at the positive and negative error centers are almost exactly uncorrelated with each other.

One way for a LIM to fail is if its state vector $x$ is
incomplete. One might suspect, for instance, that the underestimated persistence of tropical heating (see Fig. 3) is partly due to not explicitly including tropical SST in the model. Could this reduce the extratropical persistence as well? To address this question, a new LIM was constructed by extending the state vector with tropical SST components. Specifically, 7-day running mean anomalies of tropical skin temperatures $S$ from the NCEP reanalysis were projected onto their EOFs, and the PCs of the leading 15 EOFs (explaining about 70% of the weekly variance) were included in $x$. This new model improved the 21-day forecast skill of heating throughout the tropics, and to a lesser extent also the $\psi_{250}$ forecast skill throughout the hemisphere. It also produced much-improved lag covariances of tropical heating. Figure 14 shows the observed and predicted lag-autocorrelation functions of the leading PCs of each model variable. Note that, by construction, they are identical at the 5-day training lag. Also shown are 90% confidence intervals estimated using the Monte Carlo procedure described above. Without $S$ in the LIM, the heating autocorrelation decays too rapidly with lag and soon lies outside the confidence interval.

Unfortunately, including $S$ in $x$ does not remove the problem in the SLP fields in Fig. 13. It does slightly improve North Pacific forecast skill but not over the

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**Fig. 12.** Day-35 (top) $p$ and (bottom) $\psi_{30}$ response to the leading singular vector for a 35-day lag: the norm is the amplification of the leading $p$ EOF. (left) Anomalies evolved using the full LIM; (right) anomalies evolved without tropical influences, e.g., evolved by $L_{\text{noh}}$. Contour intervals are (top) 10 Pa and (bottom) $3.75 \times 10^5$ m$^2$ s$^{-1}$; contours/shading as in Fig. 9.
North Atlantic and Arctic regions where the skill is actually slightly degraded. Also, although the persistence of $p$ PC1 is enhanced (Fig. 14), the oscillating component of the autocorrelation function (Ambaum and Hoskins 2002) is still not reproduced.

Two other variables, nonland skin temperature north of $60^\circ$N and column-integrated tropospheric diabatic heating north of $30^\circ$N, were also used in attempts to improve the LIM. Each was separately included in $x$, retaining sufficient PCs to explain about 75% of the polar skin temperature and 59% of the extratropical heating weekly variances, but in both cases there was minimal impact on both forecast skill and the autocorrelation function.

The basic reason for our LIM's error in Fig. 13 may simply be that its assumptions are less valid over the North Atlantic. Since this is apparently a region of strong interaction between the surface and the stratosphere, any substantial seasonality in those interactions (associated with, say, the seasonality of tropopause heights) or in stratospheric variability [associated with, e.g., stratospheric sudden warmings that occur much more rarely in December, Charlton and Polvani (2007)] would invalidate the LIM's basic assumption of statistical stationarity. One indication of seasonality is that the correlation between the leading SLP and stratospheric PCs is 0.33 in January but only 0.16 in December and 0.08 in February.

Nonlinear dynamical interactions in the North Atlantic may, of course, also decorrelate too slowly for any LIM to work. One might suspect this from the climatology of isentropic potential vorticity (PV) in the upper troposphere (see, e.g., the wintertime 330 K PV surface in the NCEP-NCAR reanalysis atlas, which is

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**Fig. 13.** Difference between observed and LIM-predicted (left) 28-day and (right) 35-day lag covariances for (top) $\psi_{250}$ and (bottom) $p$: Positive (negative) values indicated by thick (thin) contours; contour intervals as in Fig. 3. Gray shading indicates where the LIM lag covariance does not lie within the 90% confidence interval for the observed lag covariance based on a Monte Carlo test; refer to text.
available online at http://www.cdc.noaa.gov/cgi-bin/DataMenus.pl?dataset=NCEP; Scott et al. 1997). The PV gradient over the eastern Atlantic is weaker than the gradient over the eastern Pacific, indicative of stronger wave breaking and PV mixing that may occur too slowly to be approximated as white noise in a LIM constructed from weekly averages. Still, it is intriguing that Charlton et al. (2003) found only very weak nonlinear relationships between daily wintertime values of the AO at 1000 and 70 hPa. Nonlinearity need not be only due to upper-tropospheric wave breaking, of course. For example, distant ENSO forcing can produce subtly different responses over the North Pacific to warm versus cold ENSO events that are further amplified downstream over the North Atlantic (Sardeshmukh et al. 2000; Brönnimann 2007). Also, possibly asymmetric stratospheric responses to the warm versus cold phases of ENSO (e.g., Taguchi and Hartmann 2006; Manzini et al. 2006; Wei et al. 2007) may result in asymmetric stratospheric feedbacks onto the polar SLP. Finally, our analysis has neglected nonlinear surface interactions, especially those involving high-latitude sea ice and SST variations (e.g., Alexander et al. 2004; Deser et al. 2004), which would be particularly consistent with the regional confinement and shallowness of the LIM’s persistence error.

Fig. 14. Comparison of the autocorrelation function of the leading principal component of each model variable for observations (solid line) and the LIM (dashed line). Gray shading indicates the 90% confidence interval for the observed autocorrelation based on a Monte Carlo test. Results obtained using an extended LIM with additional tropical oceanic skin temperature components shown as dashed–dotted lines.
8. Summary and concluding remarks

It is a truism that correlation does not imply causation, and mere documentations of correlations and lag correlations do not establish dynamical relationships between a system’s variables. Linear inverse modeling goes beyond this by estimating from observations an effectively linear dynamical feedback matrix $L$ encapsulating the dynamical relationships. Its key assumption is that the system’s lag covariance matrices at different lags are linked as $C(\tau) = \exp(L\tau)C(0)$. It uses this relationship to estimate $L$ from one lag and then tests it at other lags (this is the “tau test” of Penland and Sardeshmukh 1995). Successful passage of the tau test justifies extensive dynamical diagnosis of the system through investigation of the structure and properties of $L$, as done here. The tau test can fail if one has not included all dynamically active agents in the analysis, if the statistics are not stationary, or if the dynamics are not even effectively linear (i.e., if the nonlinear interactions cannot be approximated as linear terms plus stochastic noise). Dynamical diagnosis of a system from observed linear correlations is, therefore, either importantly incomplete (even if the dynamics are effectively linear) or inadequate if the tau test fails.

In this study, our focus was on elucidating the relative impacts of tropical diabatic heating and stratospheric circulation anomalies on the extratropical tropospheric circulation anomalies in winter. To this end, we constructed a LIM from the zero-lag and 5-day lag covariances of the observed 7-day running mean anomalies. To justify our linear diagnosis, we performed the tau test and successfully demonstrated the LIM’s ability to reproduce the observed lag covariance statistics at lags other than the lag on which the LIM was trained. We then analyzed interactions among the LIM variables by shutting off some of them in the LIM $L$ operator and also by examining the forecast impacts of setting some components of the initial conditions to zero. Our demonstration that the dynamics of weekly averages are effectively linear and stochastically driven also enabled a second-order closure of the moment equations, in particular a meaningful discussion of the streamfunction variance budget. It additionally justified a meaningful singular vector analysis of the system’s propagator $\exp(L\tau)$, which shed further light on the tropical and stratospheric influences on extratropical tropospheric circulation variability and predictability.

As a result of this diagnosis, we conclude that tropical diabatic heating greatly enhances persistent variability over most of the Northern Hemisphere, especially over the Pacific and North America, whereas stratospheric effects are largely confined to the polar region. Over the North Atlantic both effects are important, although our results also suggest that some indirect tropical effects could be mistaken for direct stratospheric influences. Even in the absence of these “external” tropical and stratospheric influences, however, some persistent variability remains that can be linked to the leading eigenmodes of the LIM’s internal extratropical tropospheric evolution operator. The two eigenmodes associated with north–south dipole variations across the North Atlantic represent the implicit inclusion in $L$ of linear synoptic-eddy feedbacks on the slowly varying circulation (e.g., Gerber and Vallis 2007). The eigenmode with a circumboreal zonal wave-number-5 structure is suggestive of a quasi-stationary barotropic mode in the Pacific waveguide (Branstator 2002) and enhances persistence near the date line. None of the leading eigenmodes of the internal operator, however, are eigenmodes of the full operator, raising the possibility that coupling to the tropics and stratosphere does not merely act to select some extratropical modes over others, but also modifies the modes themselves.

In general, we find that tropically forced anomalies extend through the depth of the troposphere and into the stratosphere, whereas stratospherically generated anomalies tend to be largest at the surface and relatively weak at midtropospheric levels. The relative confinement of the stratospheric influence to the North Atlantic and Arctic is consistent with the view that it is associated with large PV anomalies at and above the tropopause (e.g., Ambaum and Hoskins 2002). These anomalies have a surface footprint induced by balanced PV dynamics that is relatively large when the tropopause is closer to the surface near Scandinavia, Greenland, and Siberia. The midtropospheric variability driven by tropical heating is associated with weaker PV anomalies and a correspondingly smaller surface impact.

As a related consequence, our results suggest that, while the classic NAO with opposing centers of action over Iceland and the Azores is a largely tropospheric phenomenon driven by synoptic-eddy feedbacks and, to a lesser extent, tropical heating, the stratospheric anomalies generated by the NAO then feedback onto the remainder of the polar region, producing the more zonally symmetric AO pattern associated with $\mathbf{p}/\text{EOF}_1$. Kodera and Kuroda 2004 made a somewhat similar distinction.) One might, therefore, expect studies that are based upon the time series of a single NAO or AO pattern to have difficulty distinguishing stratospheric from tropical effects.

Past studies considering relationships between the
tropics and the extratropical stratosphere have typically focused on ENSO-related tropical SST forcing. WNS01 emphasized the somewhat obvious point that ultimately the extratropical response to tropical forcing depends on the evolving tropical heating anomalies and not the SST anomalies themselves. In our study, too, the heating pattern contributing to the greatest possible stratospheric anomaly amplification over a month is similar, but not identical, to the canonical ENSO heating anomaly pattern (e.g., cf. Figs. 1 and 11), and there are also important differences between these and the initial heating pattern associated with the greatest impact over the Atlantic.

Finally, although our focus here was on tropical and stratospheric influences on extratropical tropospheric variability, our LIM also allows investigations of influences in the reverse direction, which we did not pursue here. The influence on tropical heating, in particular, is a relatively unexplored territory. Sardeshmukh and Sura (2007) recently showed a strong impact of low-frequency extratropical anomalies on the thermal structure of the tropical troposphere on longer time scales. To what extent this impacts tropical heating variability is an intriguing question.

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